

1. Find the work done by each \mathbf{F} below from $(0, 0, 0)$ to $(1, 1, 1)$ over each of the following paths:

- The straight line segment.
- The curve $t\mathbf{i} + t^2\mathbf{j} + t^4\mathbf{k}$
- First the line segment from $(0, 0, 0)$ to $(1, 1, 0)$ and then the line segment from $(1, 1, 0)$ to $(1, 1, 1)$

(a) $\mathbf{F} = 3y\mathbf{i} + 2x\mathbf{j} + 4z\mathbf{k}$

(b) $\mathbf{F} = (3x^2 - 3)\mathbf{i} + 3z\mathbf{j} + \mathbf{k}$

(c) $\mathbf{F} = (e^x \cos y)\mathbf{i} - (e^x \sin y)\mathbf{j} + z\mathbf{k}$

(d) $\mathbf{F} = e^{y+2z}(\mathbf{i} + x\mathbf{j} + 2x\mathbf{k})$

2. How are each of the following related?

(a) $\int_{\gamma} \mathbf{F} \cdot d\mathbf{s}$ and $\int_{-\gamma} \mathbf{F} \cdot d\mathbf{s}$

(b) $\int_{\gamma} f ds$ and $\int_{-\gamma} f ds$

3. Evaluate $\int_C (x - y) dx + (x + y) dy$ counterclockwise around the triangle with vertices $(0, 0)$, $(1, 0)$, and $(0, 1)$.

4. Find the divergence and curl of the vector fields in problem 1.

5. Given a vector field \mathbf{F} , find the divergence of the curl of \mathbf{F} . (If you did this on the homework, you do not have to repeat it!)

6. Consider the field

$$\mathbf{F} = xy\mathbf{i} + y\mathbf{j} - yz\mathbf{k}$$

Find the work done by this vector field from $(0, 0, 0)$ to $(1, 1, 1)$ along the curve of intersection of the parabolic cylinder $y = x^2$ and the plane $z = x$. (Hint: Use $t = x$ as the parameter.)

7. (a) $\int_A^B z^2 dx + 2y dy + 2xz dz$

(b) $\int_A^B \frac{x dx + y dy + z dz}{\sqrt{x^2 + y^2 + z^2}}$