

1. Match the vector fields below with their equations.

(a)  $\mathbf{F}(x, y) = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$

(b)  $\mathbf{F}(x, y) = \begin{pmatrix} \frac{x}{\sqrt{x^2+y^2}} \\ \frac{y}{\sqrt{x^2+y^2}} \end{pmatrix}$

(c)  $\mathbf{F}(x, y) = \begin{pmatrix} \frac{y}{\sqrt{x^2+y^2}} \\ \frac{-x}{\sqrt{x^2+y^2}} \end{pmatrix}$

(d)  $\mathbf{F}(x, y) = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$

(e)  $\mathbf{F}(x, y) = \begin{pmatrix} \frac{y}{x^2+y^2} \\ \frac{-x}{x^2+y^2} \end{pmatrix}$

(f)  $\mathbf{F}(x, y) = \begin{pmatrix} y \\ -x \end{pmatrix}$

(g)  $\mathbf{F}(x, y) = \begin{pmatrix} -x \\ 0 \end{pmatrix}$

(h)  $\mathbf{F}(x, y) = \begin{pmatrix} \frac{-y}{x^2+y^2} + \frac{-y}{(x-1)^2+y^2} \\ \frac{x}{x^2+y^2} + \frac{x-1}{(x-1)x^2+y^2} \end{pmatrix}$

(i)  $\mathbf{F}(x, y) = \begin{pmatrix} \frac{x}{(\sqrt{x^2+y^2})^3} \\ \frac{y}{(\sqrt{x^2+y^2})^3} \end{pmatrix}$

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2. For each, decide whether the divergence is positive, negative, or zero by looking at the vector field. Verify by calculating the divergence for parts (a), (d), (e), (f), and (g).

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3. For each, decide whether the curl around the  $z$ -axis is positive, negative, or 0. Verify by calculating  $Q_x - P_y$  for (a), (d), (e), (f), and (g).

