

**Exercises 14:** 5, 6, 7, 13, 14, 25, 31, 34

**Exercises 15:** 3, 4, 7, 9

**Additional exercises:**

1. Recall that  $SL_n(\mathbb{R}) = \{A \in GL_n(\mathbb{R}) \mid \det(A) = 1\}$ . Prove that  $SL_n(\mathbb{R})$  is a subgroup of  $GL_n(\mathbb{R})$ . Then prove that it is a normal subgroup in two different ways:
  - (a) first, using the fact that  $H$  is a normal subgroup of  $G$  if and only if  $N_G(H) = G$ .
  - (b) second, by finding a map from  $GL_n(\mathbb{R})$  to a group such that  $SL_n(\mathbb{R})$  is the kernel of the map. (Hint: Use the definition of  $SL_n(\mathbb{R})$  to help you find this map.)