

1. Consider the torus, Σ , which is the circle in the xz -plane centered at $x = 5$ and $z = 0$ with radius 3 rotated about the z -axis to form a donut-like shape. Σ has the parametrization $f(t, u) = ((5 + 3 \cos t) \cos u, (5 + 3 \cos t) \sin u, 3 \sin t)$.

(a) Find the surface area of Σ .

(b) Set up an integral to find $\int_{\Sigma} z^2 d\sigma$.

2. Let Σ be the surface defined by the equations $x^2 + y^2 = 9, 0 \leq z \leq 4$. Evaluate $\int_{\Sigma} (x + y + z) d\sigma$.

3. Compute $\int_{\Sigma} z d\sigma$ where Σ is the disk $x^2 + y^2 \leq 4$ on the plane $z = 3$.

4. Compute the following surface integrals:

(a) $\int_{\Sigma} x^2 y z d\sigma$, where Σ is the part of the plane $z = 1 + 2x + 3y$ that lies above the rectangle $0 \leq x \leq 3, 0 \leq y \leq 2$.

(b) $\int_{\Sigma} y z d\sigma$, where Σ is the part of the plane $x + y + z = 1$ that lies in the first octant.

(c) $\int_{\Sigma} y z d\sigma$, where Σ is the part of the plane $z = y + 3$ that lies inside the cylinder $x^2 + y^2 = 1$.

(d) $\int_{\Sigma} z d\sigma$, where Σ is the hemisphere $x^2 + y^2 + z^2 = 4, z \geq 0$.

5. Find the mass of the $x^2 + y^2 + z^2 = 4, z \geq 0$ if it has constant density $\rho = a$.