- 1. $\langle 6,7 \rangle$; $\langle -7,6 \rangle$ and $\langle 7,-6 \rangle$.
- 2. $(2/\sqrt{13}, -3/\sqrt{13})$ and $(-2/\sqrt{13}, 3/\sqrt{13})$.
- 3. From the implicit function theorem, we know that if $\frac{\partial f}{\partial y} \neq 0$, then the zero set of f defines y as a function of x. Since, near (0,0), the graph does not pass the vertical line test, y is not a function of x, so $\frac{\partial f}{\partial y} = 0$. Similarly, the graph does not pass the horizontal line test, so $\frac{\partial f}{\partial x} = 0$. Thus, $\vec{\nabla}f = \vec{0}$, so (0,0) is a critical point.

4. When
$$y \neq 0$$
, then $\frac{\mathrm{d}y}{\mathrm{d}x} = -x/y$. When $x \neq 0$, $\frac{\mathrm{d}x}{\mathrm{d}y} = -y/x$

- 5. See solutions.
- 6. (0,0) as saddle, (0,y) a minimum for $y \neq 0$.

7. (a) Yes. g(x, y) = 0 is a closed bounded region (the curve itself), so f must attain both a global max and a global min.
(b)-(d) see graph
(e) see solutions
(f) no
(g) ⟨0,0⟩.
(h) Some critical points may occur when \$\vec{\nabla}g = 0\$, if this point lies on the level set of g, so we always need to check points (if any) where this occurs.

8. Global mx (2,3), global min (-2,3) and (2,-3).

- 9.16
- 10. 1/6
- $11.\ 32$
- $12.\ 2$